

What is claimed is:

1 1. A method for use in a parallel database system having plural nodes,
2 comprising:
3 providing random number generators in the plural nodes;
4 generating, in parallel, random numbers using the random number
5 generators in the plural nodes; and
6 performing random sampling using the generated random numbers.

1 2. The method of claim 1, wherein providing the random number generators
2 in the plural nodes comprises providing random number generators in at least some of the
3 plural nodes.

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1 7. The method of claim 5, further comprising:
2 associating the parameters with corresponding predefined ranges;
3 determining which range each random number falls within; and
4 adjusting the value of one of the parameters based on the determined range
5 of each random number.

1 8. The method of claim 7, wherein adjusting the value of the one parameter
2 comprises incrementing the value of the one parameter.

1 9. The method of claim 8, wherein incrementing the value of the one
2 parameter occurs in response to each occurrence of a random number in the determined
3 range.

4 10. The method of claim 7, further comprising communicating certain of the
5 parameters between nodes, each node determining the number of random samples
6 based on the communicated parameters.

7 11. The method of claim 1, further comprising:
8 defining plural ranges; and
9 counting a number of occurrences of random numbers in each of the plural
10 ranges.

1 12. The method of claim 11, further comprising:
2 storing plural parameters having values set to represent the number of
3 occurrences of random numbers in corresponding ranges.

1 13. The method of claim 1, further comprising:
2 generating random number seeds at one node;
3 sending the random number seeds to plural nodes from the one node; and

4 the random number generators in the plural nodes using corresponding
5 random number seeds.

1 14. A database system comprising:
2 a plurality of nodes, wherein each of at least two of the plurality of nodes
3 comprises:
4 a storage for storing tuples of a relation; and
5 a controller adapted to generate random numbers,
6 the controller adapted to determine a number of random samples to
7 generate in the node using the random numbers.

1 15. The database system of claim 14, wherein each node further comprises a
2 processor, and wherein the controller is a software program executable by the processor.

1 16. The database system of claim 14, wherein one of the nodes comprises a
2 first random number generator, and wherein each of the nodes comprises a second
3 random number generator to generate the random numbers, the first random number
4 generator to generate random number seeds for use by the second random number
5 generators.

1 17. The database system of claim 16, wherein the one node communicates the
2 random number seeds to corresponding nodes.

1 18. The database system of claim 16, wherein the plural nodes comprise nodes
2 i , $i = 1 - L$, wherein the first random number generator is adapted to generate random
3 number seeds s_i , $i = 1 - L$, and wherein the one node is adapted to send each random
4 number seed s_i to node i .

1 19. The database system of claim 18, wherein the second random number
2 generator in each node i is adapted to generate random numbers $r_1 \dots r_{M_i}$, where M_i
3 represents a number of random numbers to be generated in node i .

1 20. The database system of claim 19, the storage in each node i to store array
2 elements $A_{i1} \dots A_{iL}$, the controller adapted to adjust the value of A_{ij} , j equal to a value
3 between 1 and L , based on which of plural predefined ranges each random number r falls
4 within.

1 21. The database system of claim 20, wherein each node is adapted to
2 communicate certain of these array elements to other nodes.

1 22. The database system of claim 21, wherein the controller in each node is
2 adapted to sum values of the array elements to derive the number of random samples to
3 generate.

1 23. An article comprising at least one storage medium storing instructions that
2 when executed cause a database system to:

3 generate random numbers in each of plural nodes of the database system;

4 and

5 use the random numbers to determine a number of random samples to
6 generate in each node.

1 24. The article of claim 23, wherein the instructions when executed cause the
2 database system to provide a first random number generator in each node to generate the
3 random numbers.

1 25. The article of claim 24, wherein the instructions when executed cause the
2 database system to provide a second random number generator in one of the nodes to
3 generate random number seeds for use by the first random number generators.

1 26. The article of claim 25, wherein the instructions when executed cause the
2 database system to distribute the random number seeds to the plural nodes.

1 27. The article of claim 23, wherein the instructions when executed cause the
2 database system to further:

3 define parameters in each node; and
4 adjust the parameters based on values of the random numbers in each
5 node, wherein determining the number of random samples is based on the parameters.

1 28. The article of claim 27, wherein the instructions when executed cause the
2 database system to distribute certain of the parameters from each of the nodes to other
3 nodes.

1 29. The article of claim 28, wherein the instructions when executed cause the
2 database system to sum the parameters at each of the nodes to derive the number of
3 random samples.

1 30. An article comprising at least one storage medium storing instructions
2 executable in a database system having plural nodes, the instructions when executed
3 causing a system to: ~

4 generate random number seeds;
5 communicate the random number seeds to the plural nodes; and
6 generate random numbers in each node using at least one of the random
7 number seeds.

1 31. The article of claim 30, wherein the instructions when executed cause the
2 database system to determine a number of random samples to generate in each node
3 based on the generated random numbers.